

1-5: The Distributive Property

Example 1: Julio walks 5 days a week. He walks at a fast rate for 7 minutes and cools down for 2. Use the distributive property to write and evaluate an expression that will determine the total number of minutes Julio walks.

$$\begin{array}{l}
 \text{of minutes Julio walks.} \\
 \text{5 days/wk} \rightarrow \frac{5(7 + 2)}{5 \cdot 7 + 5 \cdot 2} \quad \begin{array}{l} \text{minutes at fast rate} \\ \text{minutes of cooldown} \end{array} \\
 \text{PEMDAS} \quad \begin{array}{c} 5 \cdot 9 \\ 45 \end{array} \quad \begin{array}{c} 35 + 10 \\ 45 \end{array} \quad \rightarrow \text{distributive property}
 \end{array}$$

Are both ways mathematically correct? yes

A Key Belief of Arithmetic

The Distributive Property: If a , b , and c are real numbers, then $a(b+c) = ab + ac$.

$$a(b-c) = ab - ac$$

Rewrite each expression using the distributive property. Then simplify.

<p>a. $7(3w - 5)$</p> <p>$7 \cdot 3w - 7 \cdot 5$</p> <p>$21w - 35$</p> <p>not like terms</p> <p>Example 2:</p>
<p>b. $(8 + 4n)2$</p> <p>$2(8 + 4n)$</p> <p>$2 \cdot 8 + 2 \cdot 4n$</p> <p>$16 + 8n$</p> <p>not like terms</p>
<p>c. $4(6x^2 + x - 3)$</p> <p>$4 \cdot 6x^2 + 4 \cdot x - 4 \cdot 3$</p> <p>$24x^2 + 4x - 12$</p> <p>not like terms</p>
<p>d. $(2 - 5q)(-3)$</p> <p>$-3(2 - 5q)$</p> <p>$-3 \cdot 2 - (-3) \cdot 5q$</p> <p>$-6 - (-15q)$</p> <p>$-6 + 15q$</p> <p>not like terms</p>

Roma says

writing $x + x = 2x$ an application of the distributive property? yes

$$x+x=1x+1x=x(1+1)=x \cdot 2 = 2x$$

This is the distributive property in reverse.

Example 3: Use the distributive property to prove that $2x + 3x = 5x$.

$$2x + 3x = x(2+3) = x \cdot 5 = 5x$$

Use the distributive property to rewrite each expression. Then evaluate.

$$\text{a. } 2(4+x)$$

$$\begin{aligned} b. \quad & (g - 9)5 = 5(g - 9) \\ & \underline{5 \cdot g - 5 \cdot 9} \\ & \quad \boxed{5g - 45} \end{aligned}$$

Simplify each expression. If not possible, write simplified.

$$\begin{array}{l} \text{a. } 13r + 5r \\ (13+5) \cdot r \\ \hline 18r \end{array}$$

b. $3x^3 + 2x^2$
not like terms
Simplified

$$c. 7m + 2m - 5p + 4m$$

$7m + 2m + 4m - 5p$

$(7+2+4) \cdot m - 5p$

$13m - 5p$

$$\begin{aligned}
 & d. \quad 3x + 7(3x + 4) \\
 & 3x + 7 \cdot 3x + 7 \cdot 4 \\
 & 3x + 21x + 28 \\
 & (3+21) \cdot x + 28 \\
 & \textcircled{24x+28}
 \end{aligned}$$

Do you remember the following definitions??? Write a definition and give an example.

Like Terms:

Terms that contain the same variables, with corresponding variables having the same exponent.

5x and 5x
like terms

5x and 20
not like terms

Simplest Form:

An expression is in simplest form when it is replaced by an equivalent expression having no like terms or parentheses. $2(x+7) = 2x + 14 \leftarrow \text{simplest form}$

Coefficient: The number in front of a variable.

\rightarrow 3 $y \leftarrow$ variable

Term: A number, a variable, or a product of numbers and variables.